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Universidad de Santiago de Chile
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Sistemas Eléctricos de Potencia

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Tarea 4: Flujo de Potencia por Método de Gauss Seidel

Resolución de Ejercicio

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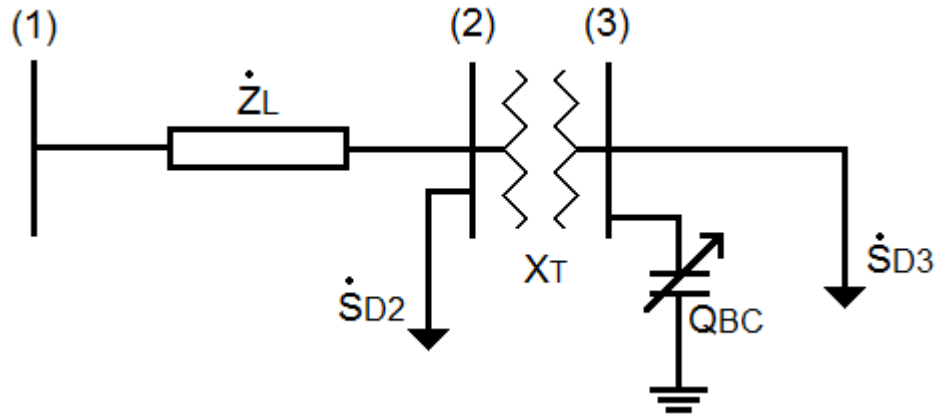
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Tarea 4: Flujo de Potencia por el Método de Gauss Seidel

Enunciado:

Para el SEP de la Figura:



Datos:

$V_1^0 = 1 \angle 0^\circ$; $V_2^0 = 1 \angle 0^\circ$; $V_3^0 = 0,95 \angle 0^\circ$
 L : $\dot{Z}_L = 0,161 + j0,327$ [p.u] ; 66 [KV] ; 100 [MVA]
 T : $X_T = 0,8 \%$; 66/ 12 [KV] ; 40 [MVA]
 C_2 : 10 [MVA] ; $\cos(\varphi) = 0,9(i)$
 C_3 : 30 [MVA] ; $\cos(\varphi) = 0,8(i)$

1. Calcular los voltajes de las Barras 2 y 3, para 10 iteraciones ($K=9$).

2. Graficar:

- La magnitud del voltaje en la Barra 2
- La magnitud del voltaje en la Barra 3
- El ángulo del voltaje en la Barra 2
- El ángulo del voltaje en la Barra 3
- La potencia reactiva Q_3
- La potencia reactiva Q_{BC}

Solución:

1.- Para llevar los parámetros del sistema a base común, dado que $S_{Base} = 100$ MVA, definimos que $S_{B1} = 66$ KV, para la línea, por tanto $Z_L(p.u)$ queda igual.

$$\dot{Z}_L(p.u) = 0,161 + j0,327 [p.u]$$

$$X_T(p.u) = X_{Ta} \cdot \left(\frac{V_{Ba}}{V_{Bn}}\right)^2 \cdot \frac{S_{Bn}}{S_{Ba}}$$

$$X_T(p.u) = 0,088 \cdot \left(\frac{66}{66}\right)^2 \cdot \frac{100}{40} = 0,22 [p.u]$$

$$\dot{S}_{D2} = \frac{10}{100} \cdot \angle \cos^{-1}(0,9) = 0,1 \angle 25,8419^\circ [p.u]$$

$$\dot{S}_{D2} = 0,09 + j0,0435 [p.u] \Rightarrow P_{D2} = 0,09 ; Q_{D2} = 0,0435$$

$$\dot{S}_{D3} = \frac{30}{100} \cdot \angle \cos^{-1}(0,8) = 0,3 \angle 36,8698^\circ [p.u]$$

$$\dot{S}_{D3} = 0,24 + j0,18 [p.u] \Rightarrow P_{D3} = 0,24 ; Q_{D3} = 0,18$$

Como existen 3 barras en el sistema, la matriz admitancias de Barra quedará de 3x3.

$$[\dot{Y}_B] = \begin{bmatrix} \dot{Y}_{11} & \dot{Y}_{12} & \dot{Y}_{13} \\ \dot{Y}_{21} & \dot{Y}_{22} & \dot{Y}_{23} \\ \dot{Y}_{31} & \dot{Y}_{32} & \dot{Y}_{33} \end{bmatrix}$$

$$\dot{Y}_{11} = \frac{1}{\dot{Z}_L} \quad ; \quad \dot{Y}_{12} = -\frac{1}{\dot{Z}_L} \quad ; \quad \dot{Y}_{13} = 0$$

$$\dot{Y}_{21} = -\frac{1}{\dot{Z}_L} \quad ; \quad \dot{Y}_{22} = \frac{1}{\dot{Z}_L} + \frac{1}{\dot{Z}_T} \quad ; \quad \dot{Y}_{23} = -\frac{1}{\dot{Z}_T}$$

$$\dot{Y}_{31} = 0 \quad ; \quad \dot{Y}_{32} = -\frac{1}{\dot{Z}_T} \quad ; \quad \dot{Y}_{33} = \frac{1}{\dot{Z}_T}$$

$$\dot{Z}_L (p.u) = 0,161 + j0,327 [p.u] \Rightarrow \frac{1}{\dot{Z}_L} = 2,7435 \angle -63,7864^\circ$$

$$jX_T (p.u) = j0,22 [p.u] \Rightarrow \frac{1}{jX_T} = j4,5454 = 4,5454 \angle -90^\circ$$

$$\frac{1}{\dot{Z}_L} + \frac{1}{jX_T} = \frac{1}{0,161 + j0,327} + \frac{1}{j0,22} = 7,1109 \angle -80,1873^\circ$$

Finalmente la Matriz Admitancias de Barra nos queda:

$$[\dot{Y}_B] = \begin{bmatrix} 2,7435 \angle -63,7864^\circ & 2,7435 \angle 116,2136^\circ & 0 \\ 2,7435 \angle 116,2136^\circ & 7,1109 \angle -80,1873^\circ & 4,5454 \angle 90^\circ \\ 0 & 4,5454 \angle 90^\circ & 4,5454 \angle -90^\circ \end{bmatrix}$$

Ahora desarrollaremos el cuadro resumen del sistema:

Barra	V	δ	P_G	Q_G	P_D	Q_D	P_N	Q_N
1	1	0	P_{G1}	Q_{G1}	0	0	$P_{G1} - 0$	$Q_{G1} - 0$
2	V_2	δ_2	0	Q_{G1}	P_{D2}	Q_{D2}	$0 - P_{D2}$	$0 - Q_{D2}$
3	0,95	δ_3	0	Q_{BC}	P_{D3}	Q_{D3}	$0 - P_{D3}$	$Q_{BC} - Q_{D3}$

Y conociendo que:

$$P_{D2} = 0,09$$

$$Q_{D2} = 0,0435$$

$$P_{D3} = 0,24$$

$$Q_{D3} = 0,18$$

Entonces remplazando los valores nos queda:

Barra	V	δ	P_G	Q_G	P_D	Q_D	P_N	Q_N
1	1	0	P_{G1}	Q_{G1}	0	0	P_{G1}	Q_{G1}
2	V_2	δ_2	0	Q_{G1}	0,09	0,0435	-0,09	-0,0435
3	0,95	δ_3	0	Q_{BC}	0,24	0,18	-0,24	$Q_{BC} - 0,18$

Tipos de Barras en este problema:

Barra	Tipo
1	Libre
2	PQ
3	PV

Ahora debemos desarrollar la Ecuación de Gauss – Seidel, para barras PQ como PV las Cuales Son:

Para barras **PQ**:

$$\dot{V}_p^{(k+1)} = \frac{1}{\dot{Y}_{pp}} \cdot \left[\left(\frac{\dot{S}_p}{\dot{V}_p^{(k)}} \right)^* - \sum_{q=1}^{p-1} \dot{Y}_{pq} \cdot \dot{V}_q^{(k+1)} - \sum_{q=p+1}^n \dot{Y}_{pq} \cdot \dot{V}_q^{(k)} \right]$$

Cuando existen barras **PV**, hay que trabajar con estas 2 ecuaciones:

$$Q_p^{(k+1)} = -Im \left[\left(\dot{V}_p^{(k)} \right)^* \cdot \left(\sum_{q=1}^{p-1} \dot{Y}_{pq} \cdot \dot{V}_q^{(k+1)} + \sum_{q=p}^n \dot{Y}_{pq} \cdot \dot{V}_q^{(k)} \right) \right]$$

$$\dot{V}_p^{(k+1)} = \frac{1}{\dot{Y}_{pp}} \cdot \left[\left(\frac{\dot{S}_p^{(k+1)}}{\dot{V}_p^{(k)}} \right)^* - \sum_{q=1}^{p-1} \dot{Y}_{pq} \cdot \dot{V}_q^{(k+1)} - \sum_{q=p+1}^n \dot{Y}_{pq} \cdot \dot{V}_q^{(k)} \right]$$

Para la Barra 2 (Barra PQ), nos queda:

$$\dot{V}_p^{(k+1)} = \frac{1}{\dot{Y}_{pp}} \cdot \left[\left(\frac{\dot{S}_p}{\dot{V}_p^{(k)}} \right)^* - \sum_{q=1}^{p-1} \dot{Y}_{pq} \cdot \dot{V}_q^{(k+1)} - \sum_{q=p+1}^n \dot{Y}_{pq} \cdot \dot{V}_q^{(k)} \right]$$

$$\dot{V}_2^{(k+1)} = \frac{1}{\dot{Y}_{22}} \cdot \left[\left(\frac{\dot{S}_2}{\dot{V}_2^{(k)}} \right)^* - \sum_{q=1}^{2-1} \dot{Y}_{2q} \cdot \dot{V}_q^{(k+1)} - \sum_{q=2+1}^3 \dot{Y}_{2q} \cdot \dot{V}_q^{(k)} \right]$$

$$\dot{V}_2^{(k+1)} = \frac{1}{\dot{Y}_{22}} \cdot \left[\left(\frac{\dot{S}_2}{\dot{V}_2^{(k)}} \right)^* - \sum_{q=1}^1 \dot{Y}_{2q} \cdot \dot{V}_q^{(k+1)} - \sum_{q=3}^3 \dot{Y}_{2q} \cdot \dot{V}_q^{(k)} \right]$$

$$\dot{V}_2^{(k+1)} = \frac{1}{\dot{Y}_{22}} \cdot \left[\left(\frac{\dot{S}_2}{\dot{V}_2^{(k)}} \right)^* - \dot{Y}_{21} \cdot \dot{V}_1^{(k+1)} - \left(\dot{Y}_{23} \cdot \dot{V}_3^{(k)} \right) \right]$$

Quedando la ecuación de voltajes en la **Barra 2** para k iteraciones, así:

$$\dot{V}_2^{(k+1)} = \frac{1}{\dot{Y}_{22}} \cdot \left[\left(\frac{\dot{S}_2}{\dot{V}_2^{(k)}} \right)^* - \dot{Y}_{21} \cdot \dot{V}_1^{(k+1)} - \dot{Y}_{23} \cdot \dot{V}_3^{(k)} \right]$$

Para la Barra 3 (Barra PV), aquí necesitaremos el cálculo previo de Q:

$$Q_3^{(k+1)} = -Im \left[\left(\dot{V}_3^{(k)} \right)^* \cdot \left(\sum_{q=1}^{3-1} \dot{Y}_{3q} \cdot \dot{V}_q^{(k+1)} + \sum_{q=3}^3 \dot{Y}_{3q} \cdot \dot{V}_q^{(k)} \right) \right]$$

$$Q_3^{(k+1)} = -Im \left[\left(\dot{V}_3^{(k)} \right)^* \cdot \left(\sum_{q=1}^2 \dot{Y}_{3q} \cdot \dot{V}_q^{(k+1)} + \sum_{q=3}^3 \dot{Y}_{3q} \cdot \dot{V}_q^{(k)} \right) \right]$$

En este punto obtenemos la Potencia Reactiva que necesitamos:

$$Q_3^{(k+1)} = -Im \left[\left(\dot{V}_3^{(k)} \right)^* \cdot \left(\dot{Y}_{31} \cdot \dot{V}_1^{(k+1)} + \dot{Y}_{32} \cdot \dot{V}_2^{(k+1)} + \dot{Y}_{33} \cdot \dot{V}_3^{(k)} \right) \right]$$

Ahora podemos desarrollar los voltajes de Barras según la primera ecuación:

$$\dot{V}_3^{(k+1)} = \frac{1}{\dot{Y}_{33}} \cdot \left[\left(\frac{\dot{S}_3}{\dot{V}_3^{(k)}} \right)^* - \sum_{q=1}^{3-1} \dot{Y}_{3q} \cdot \dot{V}_q^{(k+1)} - \sum_{q=3+1}^3 \dot{Y}_{3q} \cdot \dot{V}_q^{(k)} \right]$$

$$\dot{V}_3^{(k+1)} = \frac{1}{\dot{Y}_{33}} \cdot \left[\left(\frac{\dot{S}_3}{\dot{V}_3^{(k)}} \right)^* - \sum_{q=1}^2 \dot{Y}_{3q} \cdot \dot{V}_q^{(k+1)} - \sum_{q=4}^3 \dot{Y}_{3q} \cdot \dot{V}_q^{(k)} \right]$$

$$\dot{V}_3^{(k+1)} = \frac{1}{\dot{Y}_{33}} \cdot \left[\left(\frac{\dot{S}_3}{\dot{V}_3^{(k)}} \right)^* - \left(\dot{Y}_{31} \cdot \dot{V}_1^{(k+1)} + \dot{Y}_{32} \cdot \dot{V}_2^{(k+1)} \right) \right]$$

Quedando la ecuación de voltajes en la **Barra 3** para k iteraciones, así:

$$\dot{V}_3^{(k+1)} = \frac{1}{\dot{Y}_{33}} \cdot \left[\left(\frac{\dot{S}_3}{\dot{V}_3^{(k)}} \right)^* - \dot{Y}_{31} \cdot \dot{V}_1^{(k+1)} - \dot{Y}_{32} \cdot \dot{V}_2^{(k+1)} \right]$$

Iniciaremos las iteraciones con $K = 0$ y llegaremos a $K = 9$, es decir, realizaremos 10 iteraciones.

Para $K = 0$, nos queda:

$$V_1^0 = 1\angle 0^\circ \quad ; \quad V_2^0 = 1\angle 0^\circ \quad ; \quad V_3^0 = 0,95\angle 0^\circ$$

Y conociendo que:

$$V_1^0 = V_1^1 = V_1^2 = \dots = V_1^{(k)} = V_1^{(k+1)} = 1\angle 0^\circ$$

Desarrollaremos la iteración:

$$\dot{V}_p^{(k+1)} = \frac{1}{\dot{Y}_{pp}} \cdot \left[\left(\frac{\dot{S}_p}{\dot{V}_p^{(k)}} \right)^* - \sum_{q=1}^{p-1} \dot{Y}_{pq} \cdot \dot{V}_q^{(k+1)} - \sum_{q=p+1}^n \dot{Y}_{pq} \cdot \dot{V}_q^{(k)} \right]$$

$$\dot{V}_2^{(1)} = \frac{1}{\dot{Y}_{22}} \cdot \left[\left(\frac{\dot{S}_2}{\dot{V}_2^{(0)}} \right)^* - \sum_{q=1}^1 \dot{Y}_{2q} \cdot \dot{V}_q^{(1)} - \sum_{q=3}^3 \dot{Y}_{2q} \cdot \dot{V}_q^{(0)} \right]$$

$$\dot{V}_2^{(1)} = \frac{1}{\dot{Y}_{22}} \cdot \left[\left(\frac{\dot{S}_2}{\dot{V}_2^{(0)}} \right)^* - \dot{Y}_{21} \cdot \dot{V}_1^{(1)} - \dot{Y}_{23} \cdot \dot{V}_3^{(0)} \right]$$

$$\dot{V}_2^{(1)} = \frac{1}{7,1109\angle -80,1873} \cdot \left[\left(\frac{-0,09 - j0,0435}{(1\angle 0)} \right)^* - (2,7435\angle 116,2136) \cdot (1\angle 0) - (4,5454\angle 90) \cdot (0,95\angle 0) \right]$$

$$\dot{V}_2^{(1)} = 0,9603\angle -0,3571 \text{ (p.u.)}$$

$$Q_p^{(k+1)} = -Im \left[\left(\dot{V}_p^{(k)} \right)^* \cdot \left(\sum_{q=1}^{p-1} \dot{Y}_{pq} \cdot \dot{V}_q^{(k+1)} + \sum_{q=p}^n \dot{Y}_{pq} \cdot \dot{V}_q^{(k)} \right) \right]$$

$$Q_3^{(1)} = -Im \left[\left(\dot{V}_3^{(0)} \right)^* \cdot \left(\sum_{q=1}^2 \dot{Y}_{3q} \cdot \dot{V}_q^{(1)} + \sum_{q=3}^3 \dot{Y}_{3q} \cdot \dot{V}_q^{(0)} \right) \right]$$

$$Q_3^{(1)} = -Im \left[\left(\dot{V}_3^{(0)} \right)^* \cdot \left(\dot{Y}_{31} \cdot \dot{V}_1^{(1)} + \dot{Y}_{32} \cdot \dot{V}_2^{(1)} + \dot{Y}_{33} \cdot \dot{V}_3^{(0)} \right) \right]$$

$$Q_3^{(1)} = -Im[(0,95\angle 0)^* \cdot (0 \cdot (1\angle 0) + (4,5454\angle 90^\circ) \cdot (0,9603\angle -0,3571) + (4,5454\angle -90) \cdot (0,95\angle 0))]$$

$$Q_3^{(1)} = -0,0444 \text{ (p.u.)}$$

$$S_3^{(k+1)} = -0,24 + jQ_3^{(k+1)}$$

$$Q_{BC}^{(k+1)} = Q_3^{(k+1)} + 0,18 \text{ (p.u.)}$$

$$Q_{BC}^{(1)} = Q_3^{(1)} + 0,18 \text{ (p.u.)} = 0,1356 \text{ (p.u.)}$$

$$S_3^{(1)} = -0,24 + jQ_3^{(1)} = -0,24 - j0,0444 \text{ (p.u.)} = 0,2440\angle -169,5187 \text{ (p.u.)}$$

$$\dot{V}_p^{(k+1)} = \frac{1}{\dot{Y}_{pp}} \cdot \left[\left(\frac{\dot{S}_p^{(k+1)}}{\dot{V}_p^{(k)}} \right)^* - \sum_{q=1}^{p-1} \dot{Y}_{pq} \cdot \dot{V}_q^{(k+1)} - \sum_{q=p+1}^n \dot{Y}_{pq} \cdot \dot{V}_q^{(k)} \right]$$

$$\dot{V}_3^{(1)} = \frac{1}{\dot{Y}_{33}} \cdot \left[\left(\frac{\dot{S}_3^{(1)}}{\dot{V}_3^{(0)}} \right)^* - \sum_{q=1}^2 \dot{Y}_{3q} \cdot \dot{V}_q^{(1)} - \sum_{q=4}^3 \dot{Y}_{3q} \cdot \dot{V}_q^{(0)} \right]$$

$$\dot{V}_3^{(1)} = \frac{1}{\dot{Y}_{33}} \cdot \left[\left(\frac{\dot{S}_3^{(1)}}{\dot{V}_3^{(0)}} \right)^* - \dot{Y}_{31} \cdot \dot{V}_1^{(1)} - \dot{Y}_{32} \cdot \dot{V}_2^{(1)} \right]$$

$$\dot{V}_3^{(1)} = \frac{1}{4,5454\angle -90} \cdot \left[\left(\frac{-0,24 - j0,0444}{0,95\angle 0} \right)^* - 0 \cdot (1\angle 0) - (4,5454\angle 90) \cdot (0,9603\angle -0,3571) \right]$$

$$\dot{V}_3^{(1)} = 0,9520\angle -3,7079$$

Por lo tanto:

$$\dot{V}_3^{(1)} = 0,95\angle -3,7079 \text{ (p.u)}$$

$$\dot{V}_2^{(1)} = 0,9603\angle - 0,3571 \text{ (p.u)}$$

$$\dot{V}_3^{(1)} = 0.95\angle - 3,7079 \text{ (p.u)}$$

Para K = 1, nos queda:

$$\dot{V}_p^{(k+1)} = \frac{1}{\dot{Y}_{pp}} \cdot \left[\left(\frac{\dot{S}_p}{\dot{V}_p^{(k)}} \right)^* - \sum_{q=1}^{p-1} \dot{Y}_{pq} \cdot \dot{V}_q^{(k+1)} - \sum_{q=p+1}^n \dot{Y}_{pq} \cdot \dot{V}_q^{(k)} \right]$$

$$\dot{V}_2^{(2)} = \frac{1}{\dot{Y}_{22}} \cdot \left[\left(\frac{\dot{S}_2}{\dot{V}_2^{(1)}} \right)^* - \sum_{q=1}^1 \dot{Y}_{2q} \cdot \dot{V}_q^{(2)} - \sum_{q=3}^3 \dot{Y}_{2q} \cdot \dot{V}_q^{(1)} \right]$$

$$\dot{V}_2^{(2)} = \frac{1}{\dot{Y}_{22}} \cdot \left[\left(\frac{\dot{S}_2}{\dot{V}_2^{(1)}} \right)^* - \dot{Y}_{21} \cdot \dot{V}_1^{(2)} - \dot{Y}_{23} \cdot \dot{V}_3^{(1)} \right]$$

$$\dot{V}_2^{(2)} = \frac{1}{7,1109\angle - 80,1873} \cdot \left[\left(\frac{-0,09 - j0,0435}{(0,9603\angle - 0,3571)} \right)^* - (2,7435\angle 116,2136) \cdot (1\angle 0) - (4,5454\angle 90) \cdot (0.95\angle - 3,7079) \right]$$

$$\dot{V}_2^{(2)} = 0,9530\angle - 2,6995 \text{ (p.u)}$$

$$Q_p^{(k+1)} = -Im \left[\left(\dot{V}_p^{(k)} \right)^* \cdot \left(\sum_{q=1}^{p-1} \dot{Y}_{pq} \cdot \dot{V}_q^{(k+1)} + \sum_{q=p}^n \dot{Y}_{pq} \cdot \dot{V}_q^{(k)} \right) \right]$$

$$Q_3^{(2)} = -Im \left[\left(\dot{V}_3^{(1)} \right)^* \cdot \left(\sum_{q=1}^2 \dot{Y}_{3q} \cdot \dot{V}_q^{(2)} + \sum_{q=3}^3 \dot{Y}_{3q} \cdot \dot{V}_q^{(1)} \right) \right]$$

$$Q_3^{(2)} = -Im \left[\left(\dot{V}_3^{(1)} \right)^* \cdot \left(\dot{Y}_{31} \cdot \dot{V}_1^{(2)} + \dot{Y}_{32} \cdot \dot{V}_2^{(2)} + \dot{Y}_{33} \cdot \dot{V}_3^{(1)} \right) \right]$$

$$Q_3^{(2)} = -Im[(0.95\angle - 3,7079)^* \cdot (0 \cdot (1\angle 0) + (4,5454\angle 90) \cdot (0,9530\angle - 2,6995) + (4,5454\angle - 90) \cdot (0.95\angle - 3,7079))]$$

$$Q_3^{(2)} = -0,0123 \text{ (p.u)}$$

$$S_3^{(k+1)} = -0,24 + jQ_3^{(k+1)}$$

$$Q_{BC}^{(k+1)} = Q_3^{(k+1)} + 0,18 \text{ (p.u)}$$

$$Q_{BC}^{(2)} = Q_3^{(2)} + 0,18 \text{ (p.u)} = 0,1677 \text{ (p.u)}$$

$$S_3^{(2)} = -0,24 + jQ_3^{(2)} = -0,24 - j0,0123 \text{ (p.u)} = 0,2403\angle - 177,0661 \text{ (p.u)}$$

$$\dot{V}_p^{(k+1)} = \frac{1}{\dot{Y}_{pp}} \cdot \left[\left(\frac{\dot{S}_p^{(k+1)}}{\dot{V}_p^{(k)}} \right)^* - \sum_{q=1}^{p-1} \dot{Y}_{pq} \cdot \dot{V}_q^{(k+1)} - \sum_{q=p+1}^n \dot{Y}_{pq} \cdot \dot{V}_q^{(k)} \right]$$

$$\dot{V}_3^{(2)} = \frac{1}{\dot{Y}_{33}} \cdot \left[\left(\frac{\dot{S}_3^{(2)}}{\dot{V}_3^{(1)}} \right)^* - \sum_{q=1}^2 \dot{Y}_{3q} \cdot \dot{V}_q^{(2)} - \sum_{q=4}^3 \dot{Y}_{3q} \cdot \dot{V}_q^{(1)} \right]$$

$$\dot{V}_3^{(2)} = \frac{1}{\dot{Y}_{33}} \cdot \left[\left(\frac{\dot{S}_3^{(2)}}{\dot{V}_3^{(1)}} \right)^* - \dot{Y}_{31} \cdot \dot{V}_1^{(2)} - \dot{Y}_{32} \cdot \dot{V}_2^{(2)} \right]$$

$$\dot{V}_3^{(2)} = \frac{1}{4,5454\angle -90} \cdot \left[\left(\frac{-0,24 - j0,0123}{0,95\angle -3,7079} \right)^* - 0 \cdot (1\angle 0) - (4,5454\angle 90) \cdot (0,9530\angle -2,6995) \right]$$

$$\dot{V}_3^{(2)} = 0,9508\angle -6,0471$$

Por lo tanto:

$$\dot{V}_3^{(2)} = 0,95\angle -6,0471 \text{ (p.u)}$$

$$\dot{V}_2^{(2)} = 0,9530\angle - 2,6995 \text{ (p.u)}$$

$$\dot{V}_3^{(2)} = 0,95\angle - 6,0471 \text{ (p.u)}$$

Para K = 2, nos queda:

$$\dot{V}_p^{(k+1)} = \frac{1}{\dot{Y}_{pp}} \cdot \left[\left(\frac{\dot{S}_p}{\dot{V}_p^{(k)}} \right)^* - \sum_{q=1}^{p-1} \dot{Y}_{pq} \cdot \dot{V}_q^{(k+1)} - \sum_{q=p+1}^n \dot{Y}_{pq} \cdot \dot{V}_q^{(k)} \right]$$

$$\dot{V}_2^{(3)} = \frac{1}{\dot{Y}_{22}} \cdot \left[\left(\frac{\dot{S}_2}{\dot{V}_2^{(2)}} \right)^* - \sum_{q=1}^1 \dot{Y}_{2q} \cdot \dot{V}_q^{(3)} - \sum_{q=3}^3 \dot{Y}_{2q} \cdot \dot{V}_q^{(2)} \right]$$

$$\dot{V}_2^{(3)} = \frac{1}{\dot{Y}_{22}} \cdot \left[\left(\frac{\dot{S}_2}{\dot{V}_2^{(2)}} \right)^* - \dot{Y}_{21} \cdot \dot{V}_1^{(3)} - \dot{Y}_{23} \cdot \dot{V}_3^{(2)} \right]$$

$$\dot{V}_2^{(3)} = \frac{1}{7,1109\angle - 80,1873} \cdot \left[\left(\frac{-0,09 - j0,0435}{(0,9530\angle - 2,6995)} \right)^* - (2,7435\angle 116,2136) \cdot (1\angle 0) - (4,5454\angle 90) \cdot (0,95\angle - 6,0471) \right]$$

$$\dot{V}_2^{(3)} = 0,9476\angle - 4,1509 \text{ (p.u)}$$

$$Q_p^{(k+1)} = -Im \left[\left(\dot{V}_p^{(k)} \right)^* \cdot \left(\sum_{q=1}^{p-1} \dot{Y}_{pq} \cdot \dot{V}_q^{(k+1)} + \sum_{q=p}^n \dot{Y}_{pq} \cdot \dot{V}_q^{(k)} \right) \right]$$

$$Q_3^{(3)} = -Im \left[\left(\dot{V}_3^{(2)} \right)^* \cdot \left(\sum_{q=1}^2 \dot{Y}_{3q} \cdot \dot{V}_q^{(3)} + \sum_{q=3}^3 \dot{Y}_{3q} \cdot \dot{V}_q^{(2)} \right) \right]$$

$$Q_3^{(3)} = -Im \left[\left(\dot{V}_3^{(2)} \right)^* \cdot \left(\dot{Y}_{31} \cdot \dot{V}_1^{(3)} + \dot{Y}_{32} \cdot \dot{V}_2^{(3)} + \dot{Y}_{33} \cdot \dot{V}_3^{(2)} \right) \right]$$

$$Q_3^{(3)} = -Im[(0,95\angle - 6,0471)^* \cdot (0 \cdot (1\angle 0) + (4,5454\angle 90) \cdot (0,9476\angle - 4,1509) + (4,5454\angle - 90) \cdot (0,95\angle - 6,0471))]$$

$$Q_3^{(3)} = 0,0126 \text{ (p.u)}$$

$$S_3^{(k+1)} = -0,24 + jQ_3^{(k+1)}$$

$$Q_{BC}^{(k+1)} = Q_3^{(k+1)} + 0,18 \text{ (p.u)}$$

$$Q_{BC}^{(3)} = Q_3^{(3)} + 0,18 \text{ (p.u)} = 0,1926 \text{ (p.u)}$$

$$S_3^{(3)} = -0,24 + jQ_3^{(3)} = -0,24 + j0,0126 \text{ (p.u)} = 0,2403\angle 176,9947 \text{ (p.u)}$$

$$\dot{V}_p^{(k+1)} = \frac{1}{\dot{Y}_{pp}} \cdot \left[\left(\frac{\dot{S}_p^{(k+1)}}{\dot{V}_p^{(k)}} \right)^* - \sum_{q=1}^{p-1} \dot{Y}_{pq} \cdot \dot{V}_q^{(k+1)} - \sum_{q=p+1}^n \dot{Y}_{pq} \cdot \dot{V}_q^{(k)} \right]$$

$$\dot{V}_3^{(3)} = \frac{1}{\dot{Y}_{33}} \cdot \left[\left(\frac{\dot{S}_3^{(3)}}{\dot{V}_3^{(2)}} \right)^* - \sum_{q=1}^2 \dot{Y}_{3q} \cdot \dot{V}_q^{(3)} - \sum_{q=4}^3 \dot{Y}_{3q} \cdot \dot{V}_q^{(2)} \right]$$

$$\dot{V}_3^{(3)} = \frac{1}{\dot{Y}_{33}} \cdot \left[\left(\frac{\dot{S}_3^{(3)}}{\dot{V}_3^{(2)}} \right)^* - \dot{Y}_{31} \cdot \dot{V}_1^{(3)} - \dot{Y}_{32} \cdot \dot{V}_2^{(3)} \right]$$

$$\dot{V}_3^{(3)} = \frac{1}{4,5454\angle -90} \cdot \left[\left(\frac{-0,24 + j0,0126}{0,95\angle -6,0471} \right)^* - 0 \cdot (1\angle 0) - (4,5454\angle 90) \cdot (0,9476\angle -4,1509) \right]$$

$$\dot{V}_3^{(3)} = 0,9503\angle -7,5078$$

Por lo tanto:

$$\dot{V}_3^{(3)} = 0,95\angle -7,5078 \text{ (p.u.)}$$

$$\dot{V}_2^{(3)} = 0,9476\angle - 4,1509 \text{ (p.u)}$$

$$\dot{V}_3^{(3)} = 0,95\angle - 7,5078 \text{ (p.u)}$$

Para K = 3, nos queda:

$$\dot{V}_p^{(k+1)} = \frac{1}{\dot{Y}_{pp}} \cdot \left[\left(\frac{\dot{S}_p}{\dot{V}_p^{(k)}} \right)^* - \sum_{q=1}^{p-1} \dot{Y}_{pq} \cdot \dot{V}_q^{(k+1)} - \sum_{q=p+1}^n \dot{Y}_{pq} \cdot \dot{V}_q^{(k)} \right]$$

$$\dot{V}_2^{(4)} = \frac{1}{\dot{Y}_{22}} \cdot \left[\left(\frac{\dot{S}_2}{\dot{V}_2^{(3)}} \right)^* - \sum_{q=1}^1 \dot{Y}_{2q} \cdot \dot{V}_q^{(4)} - \sum_{q=3}^3 \dot{Y}_{2q} \cdot \dot{V}_q^{(3)} \right]$$

$$\dot{V}_2^{(4)} = \frac{1}{\dot{Y}_{22}} \cdot \left[\left(\frac{\dot{S}_2}{\dot{V}_2^{(3)}} \right)^* - \dot{Y}_{21} \cdot \dot{V}_1^{(4)} - \dot{Y}_{23} \cdot \dot{V}_3^{(3)} \right]$$

$$\dot{V}_2^{(4)} = \frac{1}{7,1109\angle - 80,1873} \cdot \left[\left(\frac{-0,09 - j0,0435}{(0,9476\angle - 4,1509)} \right)^* - (2,7435\angle 116,2136) \cdot (1\angle 0) - (4,5454\angle 90) \cdot (0,95\angle - 7,5078) \right]$$

$$\dot{V}_2^{(4)} = 0,9440\angle - 5,0596 \text{ (p.u)}$$

$$Q_p^{(k+1)} = -Im \left[\left(\dot{V}_p^{(k)} \right)^* \cdot \left(\sum_{q=1}^{p-1} \dot{Y}_{pq} \cdot \dot{V}_q^{(k+1)} + \sum_{q=p}^n \dot{Y}_{pq} \cdot \dot{V}_q^{(k)} \right) \right]$$

$$Q_3^{(4)} = -Im \left[\left(\dot{V}_3^{(3)} \right)^* \cdot \left(\sum_{q=1}^2 \dot{Y}_{3q} \cdot \dot{V}_q^{(4)} + \sum_{q=3}^3 \dot{Y}_{3q} \cdot \dot{V}_q^{(3)} \right) \right]$$

$$Q_3^{(4)} = -Im \left[\left(\dot{V}_3^{(3)} \right)^* \cdot \left(\dot{Y}_{31} \cdot \dot{V}_1^{(4)} + \dot{Y}_{32} \cdot \dot{V}_2^{(4)} + \dot{Y}_{33} \cdot \dot{V}_3^{(3)} \right) \right]$$

$$Q_3^{(4)} = -Im[(0,95\angle - 7,5078)^* \cdot (0 \cdot (1\angle 0) + (4,5454\angle 90^\circ) \cdot (0,9440\angle - 5,0596) + (4,5454\angle - 90) \cdot (0,95\angle - 7,5078))]$$

$$Q_3^{(4)} = 0,0296 \text{ (p.u)}$$

$$S_3^{(k+1)} = -0,24 + jQ_3^{(k+1)}$$

$$Q_{BC}^{(k+1)} = Q_3^{(k+1)} + 0,18 \text{ (p.u)}$$

$$Q_{BC}^{(4)} = Q_3^{(4)} + 0,18 \text{ (p.u)} = 0,2096 \text{ (p.u)}$$

$$S_3^{(4)} = -0,24 + jQ_3^{(4)} = -0,24 + j0,0296 \text{ (p.u)} = 0,2418\angle 172,9690 \text{ (p.u)}$$

$$\dot{V}_p^{(k+1)} = \frac{1}{\dot{Y}_{pp}} \cdot \left[\left(\frac{\dot{S}_p^{(k+1)}}{\dot{V}_p^{(k)}} \right)^* - \sum_{q=1}^{p-1} \dot{Y}_{pq} \cdot \dot{V}_q^{(k+1)} - \sum_{q=p+1}^n \dot{Y}_{pq} \cdot \dot{V}_q^{(k)} \right]$$

$$\dot{V}_3^{(4)} = \frac{1}{\dot{Y}_{33}} \cdot \left[\left(\frac{\dot{S}_3^{(4)}}{\dot{V}_3^{(3)}} \right)^* - \sum_{q=1}^2 \dot{Y}_{3q} \cdot \dot{V}_q^{(4)} - \sum_{q=4}^3 \dot{Y}_{3q} \cdot \dot{V}_q^{(3)} \right]$$

$$\dot{V}_3^{(4)} = \frac{1}{\dot{Y}_{33}} \cdot \left[\left(\frac{\dot{S}_3^{(4)}}{\dot{V}_3^{(3)}} \right)^* - \dot{Y}_{31} \cdot \dot{V}_1^{(4)} - \dot{Y}_{32} \cdot \dot{V}_2^{(4)} \right]$$

$$\dot{V}_3^{(4)} = \frac{1}{4,5454\angle -90} \cdot \left[\left(\frac{-0,24 + j0,0296}{0,95\angle -7,5078} \right)^* - 0 \cdot (1\angle 0) - (4,5454\angle 90) \cdot (0,9440\angle -5,0596) \right]$$

$$\dot{V}_3^{(4)} = 0,9501\angle -8,4278$$

Por lo tanto:

$$\dot{V}_3^{(4)} = 0,95\angle -8,4278 \text{ (p.u.)}$$

$$\dot{V}_2^{(4)} = 0,9440\angle - 5,0596 \text{ (p.u)}$$

$$\dot{V}_3^{(4)} = 0,95\angle - 8,4278 \text{ (p.u)}$$

Para K = 4, nos queda:

$$\dot{V}_p^{(k+1)} = \frac{1}{\dot{Y}_{pp}} \cdot \left[\left(\frac{\dot{S}_p}{\dot{V}_p^{(k)}} \right)^* - \sum_{q=1}^{p-1} \dot{Y}_{pq} \cdot \dot{V}_q^{(k+1)} - \sum_{q=p+1}^n \dot{Y}_{pq} \cdot \dot{V}_q^{(k)} \right]$$

$$\dot{V}_2^{(5)} = \frac{1}{\dot{Y}_{22}} \cdot \left[\left(\frac{\dot{S}_2}{\dot{V}_2^{(4)}} \right)^* - \sum_{q=1}^1 \dot{Y}_{2q} \cdot \dot{V}_q^{(5)} - \sum_{q=3}^3 \dot{Y}_{2q} \cdot \dot{V}_q^{(4)} \right]$$

$$\dot{V}_2^{(5)} = \frac{1}{\dot{Y}_{22}} \cdot \left[\left(\frac{\dot{S}_2}{\dot{V}_2^{(4)}} \right)^* - \dot{Y}_{21} \cdot \dot{V}_1^{(5)} - \dot{Y}_{23} \cdot \dot{V}_3^{(4)} \right]$$

$$\dot{V}_2^{(5)} = \frac{1}{7,1109\angle - 80,1873} \cdot \left[\left(\frac{-0,09 - j0,0435}{(0,9440\angle - 5,0596)} \right)^* - (2,7435\angle 116,2136) \cdot (1\angle 0) - (4,5454\angle 90) \cdot (0,95\angle - 8,4278) \right]$$

$$\dot{V}_2^{(5)} = 0,9417\angle - 5,6329 \text{ (p.u)}$$

$$Q_p^{(k+1)} = -Im \left[\left(\dot{V}_p^{(k)} \right)^* \cdot \left(\sum_{q=1}^{p-1} \dot{Y}_{pq} \cdot \dot{V}_q^{(k+1)} + \sum_{q=p}^n \dot{Y}_{pq} \cdot \dot{V}_q^{(k)} \right) \right]$$

$$Q_3^{(5)} = -Im \left[\left(\dot{V}_3^{(4)} \right)^* \cdot \left(\sum_{q=1}^2 \dot{Y}_{3q} \cdot \dot{V}_q^{(5)} + \sum_{q=3}^3 \dot{Y}_{3q} \cdot \dot{V}_q^{(4)} \right) \right]$$

$$Q_3^{(5)} = -Im \left[\left(\dot{V}_3^{(4)} \right)^* \cdot \left(\dot{Y}_{31} \cdot \dot{V}_1^{(5)} + \dot{Y}_{32} \cdot \dot{V}_2^{(5)} + \dot{Y}_{33} \cdot \dot{V}_3^{(4)} \right) \right]$$

$$Q_3^{(5)} = -Im[(0,95\angle - 8,4278)^* \cdot (0 \cdot (1\angle 0) + (4,5454\angle 90^\circ) \cdot (0,9417\angle - 5,6329) + (4,5454\angle - 90) \cdot (0,95\angle - 8,4278))]$$

$$Q_3^{(5)} = 0,0407 \text{ (p.u)}$$

$$S_3^{(k+1)} = -0,24 + jQ_3^{(k+1)}$$

$$Q_{BC}^{(k+1)} = Q_3^{(k+1)} + 0,18 \text{ (p.u)}$$

$$Q_{BC}^{(5)} = Q_3^{(5)} + 0,18 \text{ (p.u)} = 0,2207 \text{ (p.u)}$$

$$S_3^{(5)} = -0,24 + jQ_3^{(5)} = -0,24 + j0,0407 \text{ (p.u)} = 0,2434\angle 170,3751 \text{ (p.u)}$$

$$\dot{V}_p^{(k+1)} = \frac{1}{\dot{Y}_{pp}} \cdot \left[\left(\frac{\dot{S}_p^{(k+1)}}{\dot{V}_p^{(k)}} \right)^* - \sum_{q=1}^{p-1} \dot{Y}_{pq} \cdot \dot{V}_q^{(k+1)} - \sum_{q=p+1}^n \dot{Y}_{pq} \cdot \dot{V}_q^{(k)} \right]$$

$$\dot{V}_3^{(5)} = \frac{1}{\dot{Y}_{33}} \cdot \left[\left(\frac{\dot{S}_3^{(5)}}{\dot{V}_3^{(4)}} \right)^* - \sum_{q=1}^2 \dot{Y}_{3q} \cdot \dot{V}_q^{(5)} - \sum_{q=4}^3 \dot{Y}_{3q} \cdot \dot{V}_q^{(4)} \right]$$

$$\dot{V}_3^{(5)} = \frac{1}{\dot{Y}_{33}} \cdot \left[\left(\frac{\dot{S}_3^{(5)}}{\dot{V}_3^{(4)}} \right)^* - \dot{Y}_{31} \cdot \dot{V}_1^{(5)} - \dot{Y}_{32} \cdot \dot{V}_2^{(5)} \right]$$

$$\dot{V}_3^{(5)} = \frac{1}{4,5454\angle -90} \cdot \left[\left(\frac{-0,24 + j0,0407}{0,95\angle -8,4278} \right)^* - 0 \cdot (1\angle 0) - (4,5454\angle 90) \cdot (0,9417\angle -5,6329) \right]$$

$$\dot{V}_3^{(5)} = 0,9501\angle -9,0105$$

Por lo tanto:

$$\dot{V}_3^{(5)} = 0.95\angle -9,0105 \text{ (p.u)}$$

$$\dot{V}_2^{(5)} = 0,9417\angle - 5,6329 (p.u)$$

$$\dot{V}_3^{(5)} = 0,95\angle - 9,0105 (p.u)$$

Para K = 5, nos queda:

$$\dot{V}_p^{(k+1)} = \frac{1}{\dot{Y}_{pp}} \cdot \left[\left(\frac{\dot{S}_p}{\dot{V}_p^{(k)}} \right)^* - \sum_{q=1}^{p-1} \dot{Y}_{pq} \cdot \dot{V}_q^{(k+1)} - \sum_{q=p+1}^n \dot{Y}_{pq} \cdot \dot{V}_q^{(k)} \right]$$

$$\dot{V}_2^{(6)} = \frac{1}{\dot{Y}_{22}} \cdot \left[\left(\frac{\dot{S}_2}{\dot{V}_2^{(5)}} \right)^* - \sum_{q=1}^1 \dot{Y}_{2q} \cdot \dot{V}_q^{(6)} - \sum_{q=3}^3 \dot{Y}_{2q} \cdot \dot{V}_q^{(5)} \right]$$

$$\dot{V}_2^{(6)} = \frac{1}{\dot{Y}_{22}} \cdot \left[\left(\frac{\dot{S}_2}{\dot{V}_2^{(5)}} \right)^* - \dot{Y}_{21} \cdot \dot{V}_1^{(6)} - \dot{Y}_{23} \cdot \dot{V}_3^{(5)} \right]$$

$$\dot{V}_2^{(6)} = \frac{1}{7,1109\angle - 80,1873} \cdot \left[\left(\frac{-0,09 - j0,0435}{(0,9417\angle - 5,6329)} \right)^* - (2,7435\angle 116,2136) \cdot (1\angle 0) - (4,5454\angle 90) \cdot (0,95\angle - 9,0105) \right]$$

$$\dot{V}_2^{(6)} = 0,9402\angle - 5,9963 (p.u)$$

$$Q_p^{(k+1)} = -Im \left[\left(\dot{V}_p^{(k)} \right)^* \cdot \left(\sum_{q=1}^{p-1} \dot{Y}_{pq} \cdot \dot{V}_q^{(k+1)} + \sum_{q=p}^n \dot{Y}_{pq} \cdot \dot{V}_q^{(k)} \right) \right]$$

$$Q_3^{(6)} = -Im \left[\left(\dot{V}_3^{(5)} \right)^* \cdot \left(\sum_{q=1}^2 \dot{Y}_{3q} \cdot \dot{V}_q^{(6)} + \sum_{q=3}^3 \dot{Y}_{3q} \cdot \dot{V}_q^{(5)} \right) \right]$$

$$Q_3^{(6)} = -Im \left[\left(\dot{V}_3^{(5)} \right)^* \cdot \left(\dot{Y}_{31} \cdot \dot{V}_1^{(6)} + \dot{Y}_{32} \cdot \dot{V}_2^{(6)} + \dot{Y}_{33} \cdot \dot{V}_3^{(5)} \right) \right]$$

$$Q_3^{(6)} = -Im[(0,95\angle - 9,0105)^* \cdot (0 \cdot (1\angle 0) + (4,5454\angle 90^\circ) \cdot (0,9402\angle - 5,9963) + (4,5454\angle - 90) \cdot (0,95\angle - 9,0105))]$$

$$Q_3^{(6)} = 0,0479 (p.u)$$

$$S_3^{(k+1)} = -0,24 + jQ_3^{(k+1)}$$

$$Q_{BC}^{(k+1)} = Q_3^{(k+1)} + 0,18 (p.u)$$

$$Q_{BC}^{(6)} = Q_3^{(6)} + 0,18 (p.u) = 0,2279 (p.u)$$

$$S_3^{(6)} = -0,24 + jQ_3^{(6)} = -0,24 + j0,0479 (p.u) = 0,2447\angle 168,7130 (p.u)$$

$$\dot{V}_p^{(k+1)} = \frac{1}{\dot{Y}_{pp}} \cdot \left[\left(\frac{\dot{S}_p^{(k+1)}}{\dot{V}_p^{(k)}} \right)^* - \sum_{q=1}^{p-1} \dot{Y}_{pq} \cdot \dot{V}_q^{(k+1)} - \sum_{q=p+1}^n \dot{Y}_{pq} \cdot \dot{V}_q^{(k)} \right]$$

$$\dot{V}_3^{(6)} = \frac{1}{\dot{Y}_{33}} \cdot \left[\left(\frac{\dot{S}_3^{(6)}}{\dot{V}_3^{(5)}} \right)^* - \sum_{q=1}^2 \dot{Y}_{3q} \cdot \dot{V}_q^{(6)} - \sum_{q=4}^3 \dot{Y}_{3q} \cdot \dot{V}_q^{(5)} \right]$$

$$\dot{V}_3^{(6)} = \frac{1}{\dot{Y}_{33}} \cdot \left[\left(\frac{\dot{S}_3^{(6)}}{\dot{V}_3^{(5)}} \right)^* - \dot{Y}_{31} \cdot \dot{V}_1^{(6)} - \dot{Y}_{32} \cdot \dot{V}_2^{(6)} \right]$$

$$\dot{V}_3^{(6)} = \frac{1}{4,5454\angle -90} \cdot \left[\left(\frac{-0,24 + j0,0479}{0,95\angle -9,0105} \right)^* - 0 \cdot (1\angle 0) - (4,5454\angle 90) \cdot (0,9402\angle -5,9963) \right]$$

$$\dot{V}_3^{(6)} = 0,9500\angle -9,3808$$

Por lo tanto:

$$\dot{V}_3^{(6)} = 0.95\angle -9,3808 \text{ (p.u.)}$$

$$\dot{V}_2^{(6)} = 0,9402\angle - 5,9963 \text{ (p.u)}$$

$$\dot{V}_3^{(6)} = 0,95\angle - 9,3808 \text{ (p.u)}$$

Para K = 6, nos queda:

$$\dot{V}_p^{(k+1)} = \frac{1}{\dot{Y}_{pp}} \cdot \left[\left(\frac{\dot{S}_p}{\dot{V}_p^{(k)}} \right)^* - \sum_{q=1}^{p-1} \dot{Y}_{pq} \cdot \dot{V}_q^{(k+1)} - \sum_{q=p+1}^n \dot{Y}_{pq} \cdot \dot{V}_q^{(k)} \right]$$

$$\dot{V}_2^{(7)} = \frac{1}{\dot{Y}_{22}} \cdot \left[\left(\frac{\dot{S}_2}{\dot{V}_2^{(6)}} \right)^* - \sum_{q=1}^1 \dot{Y}_{2q} \cdot \dot{V}_q^{(7)} - \sum_{q=3}^3 \dot{Y}_{2q} \cdot \dot{V}_q^{(6)} \right]$$

$$\dot{V}_2^{(7)} = \frac{1}{\dot{Y}_{22}} \cdot \left[\left(\frac{\dot{S}_2}{\dot{V}_2^{(6)}} \right)^* - \dot{Y}_{21} \cdot \dot{V}_1^{(7)} - \dot{Y}_{23} \cdot \dot{V}_3^{(6)} \right]$$

$$\dot{V}_2^{(7)} = \frac{1}{7,1109\angle - 80,1873} \cdot \left[\left(\frac{-0,09 - j0,0435}{(0,9402\angle - 5,9963)} \right)^* - (2,7435\angle 116,2136) \cdot (1\angle 0) - (4,5454\angle 90) \cdot (0,95\angle - 9,3808) \right]$$

$$\dot{V}_2^{(7)} = 0,9392\angle - 6,2274 \text{ (p.u)}$$

$$Q_p^{(k+1)} = -Im \left[\left(\dot{V}_p^{(k)} \right)^* \cdot \left(\sum_{q=1}^{p-1} \dot{Y}_{pq} \cdot \dot{V}_q^{(k+1)} + \sum_{q=p}^n \dot{Y}_{pq} \cdot \dot{V}_q^{(k)} \right) \right]$$

$$Q_3^{(7)} = -Im \left[\left(\dot{V}_3^{(6)} \right)^* \cdot \left(\sum_{q=1}^2 \dot{Y}_{3q} \cdot \dot{V}_q^{(7)} + \sum_{q=3}^3 \dot{Y}_{3q} \cdot \dot{V}_q^{(6)} \right) \right]$$

$$Q_3^{(7)} = -Im \left[\left(\dot{V}_3^{(6)} \right)^* \cdot \left(\dot{Y}_{31} \cdot \dot{V}_1^{(7)} + \dot{Y}_{32} \cdot \dot{V}_2^{(7)} + \dot{Y}_{33} \cdot \dot{V}_3^{(6)} \right) \right]$$

$$Q_3^{(7)} = -Im[(0,95\angle - 9,3808)^* \cdot (0 \cdot (1\angle 0) + (4,5454\angle 90^\circ) \cdot (0,9392\angle - 6,2274) + (4,5454\angle - 90) \cdot (0,95\angle - 9,3808))]$$

$$Q_3^{(7)} = 0,0528 \text{ (p.u)}$$

$$S_3^{(k+1)} = -0,24 + jQ_3^{(k+1)}$$

$$Q_{BC}^{(k+1)} = Q_3^{(k+1)} + 0,18 \text{ (p.u)}$$

$$Q_{BC}^{(7)} = Q_3^{(7)} + 0,18 \text{ (p.u)} = 0,2328 \text{ (p.u)}$$

$$S_3^{(7)} = -0,24 + jQ_3^{(7)} = -0,24 + j0,0528 \text{ (p.u)} = 0,2457\angle 167,5925 \text{ (p.u)}$$

$$\dot{V}_p^{(k+1)} = \frac{1}{\dot{Y}_{pp}} \cdot \left[\left(\frac{\dot{S}_p^{(k+1)}}{\dot{V}_p^{(k)}} \right)^* - \sum_{q=1}^{p-1} \dot{Y}_{pq} \cdot \dot{V}_q^{(k+1)} - \sum_{q=p+1}^n \dot{Y}_{pq} \cdot \dot{V}_q^{(k)} \right]$$

$$\dot{V}_3^{(7)} = \frac{1}{\dot{Y}_{33}} \cdot \left[\left(\frac{\dot{S}_3^{(7)}}{\dot{V}_3^{(6)}} \right)^* - \sum_{q=1}^2 \dot{Y}_{3q} \cdot \dot{V}_q^{(7)} - \sum_{q=4}^3 \dot{Y}_{3q} \cdot \dot{V}_q^{(6)} \right]$$

$$\dot{V}_3^{(7)} = \frac{1}{\dot{Y}_{33}} \cdot \left[\left(\frac{\dot{S}_3^{(7)}}{\dot{V}_3^{(6)}} \right)^* - \dot{Y}_{31} \cdot \dot{V}_1^{(7)} - \dot{Y}_{32} \cdot \dot{V}_2^{(7)} \right]$$

$$\dot{V}_3^{(7)} = \frac{1}{4,5454\angle -90} \cdot \left[\left(\frac{-0,24 + j0,0528}{0,95\angle -9,3808} \right)^* - 0 \cdot (1\angle 0) - (4,5454\angle 90) \cdot (0,9392\angle -6,2274) \right]$$

$$\dot{V}_3^{(7)} = 0,9500\angle -9,6169$$

Por lo tanto:

$$\dot{V}_3^{(7)} = 0.95\angle -9,6169 \text{ (p.u)}$$

$$\dot{V}_2^{(7)} = 0,9392\angle - 6,2274 \text{ (p.u)}$$

$$\dot{V}_3^{(7)} = 0,95\angle - 9,6169 \text{ (p.u)}$$

Para K = 7, nos queda:

$$\dot{V}_p^{(k+1)} = \frac{1}{\dot{Y}_{pp}} \cdot \left[\left(\frac{\dot{S}_p}{\dot{V}_p^{(k)}} \right)^* - \sum_{q=1}^{p-1} \dot{Y}_{pq} \cdot \dot{V}_q^{(k+1)} - \sum_{q=p+1}^n \dot{Y}_{pq} \cdot \dot{V}_q^{(k)} \right]$$

$$\dot{V}_2^{(8)} = \frac{1}{\dot{Y}_{22}} \cdot \left[\left(\frac{\dot{S}_2}{\dot{V}_2^{(7)}} \right)^* - \sum_{q=1}^1 \dot{Y}_{2q} \cdot \dot{V}_q^{(8)} - \sum_{q=3}^3 \dot{Y}_{2q} \cdot \dot{V}_q^{(7)} \right]$$

$$\dot{V}_2^{(8)} = \frac{1}{\dot{Y}_{22}} \cdot \left[\left(\frac{\dot{S}_2}{\dot{V}_2^{(7)}} \right)^* - \dot{Y}_{21} \cdot \dot{V}_1^{(8)} - \dot{Y}_{23} \cdot \dot{V}_3^{(7)} \right]$$

$$\dot{V}_2^{(8)} = \frac{1}{7,1109\angle - 80,1873} \cdot \left[\left(\frac{-0,09 - j0,0435}{(0,9392\angle - 6,2274)} \right)^* - (2,7435\angle 116,2136) \cdot (1\angle 0) - (4,5454\angle 90) \cdot (0,95\angle - 9,6169) \right]$$

$$\dot{V}_2^{(8)} = 0,9386\angle - 6,3748 \text{ (p.u)}$$

$$Q_p^{(k+1)} = -Im \left[\left(\dot{V}_p^{(k)} \right)^* \cdot \left(\sum_{q=1}^{p-1} \dot{Y}_{pq} \cdot \dot{V}_q^{(k+1)} + \sum_{q=p}^n \dot{Y}_{pq} \cdot \dot{V}_q^{(k)} \right) \right]$$

$$Q_3^{(8)} = -Im \left[\left(\dot{V}_3^{(7)} \right)^* \cdot \left(\sum_{q=1}^2 \dot{Y}_{3q} \cdot \dot{V}_q^{(8)} + \sum_{q=3}^3 \dot{Y}_{3q} \cdot \dot{V}_q^{(7)} \right) \right]$$

$$Q_3^{(8)} = -Im \left[\left(\dot{V}_3^{(7)} \right)^* \cdot \left(\dot{Y}_{31} \cdot \dot{V}_1^{(8)} + \dot{Y}_{32} \cdot \dot{V}_2^{(8)} + \dot{Y}_{33} \cdot \dot{V}_3^{(7)} \right) \right]$$

$$Q_3^{(8)} = -Im[(0,95\angle - 9,6169)^* \cdot (0 \cdot (1\angle 0) + (4,5454\angle 90^\circ) \cdot (0,9386\angle - 6,3748) + (4,5454\angle - 90) \cdot (0,95\angle - 9,6169))]$$

$$Q_3^{(8)} = 0,0557 \text{ (p.u)}$$

$$S_3^{(k+1)} = -0,24 + jQ_3^{(k+1)}$$

$$Q_{BC}^{(k+1)} = Q_3^{(k+1)} + 0,18 \text{ (p.u)}$$

$$Q_{BC}^{(8)} = Q_3^{(8)} + 0,18 \text{ (p.u)} = 0,2357 \text{ (p.u)}$$

$$S_3^{(8)} = -0,24 + jQ_3^{(8)} = -0,24 + j0,0557 \text{ (p.u)} = 0,2463\angle 166,9339 \text{ (p.u)}$$

$$\dot{V}_p^{(k+1)} = \frac{1}{\dot{Y}_{pp}} \cdot \left[\left(\frac{\dot{S}_p^{(k+1)}}{\dot{V}_p^{(k)}} \right)^* - \sum_{q=1}^{p-1} \dot{Y}_{pq} \cdot \dot{V}_q^{(k+1)} - \sum_{q=p+1}^n \dot{Y}_{pq} \cdot \dot{V}_q^{(k)} \right]$$

$$\dot{V}_3^{(8)} = \frac{1}{\dot{Y}_{33}} \cdot \left[\left(\frac{\dot{S}_3^{(8)}}{\dot{V}_3^{(7)}} \right)^* - \sum_{q=1}^2 \dot{Y}_{3q} \cdot \dot{V}_q^{(8)} - \sum_{q=4}^3 \dot{Y}_{3q} \cdot \dot{V}_q^{(7)} \right]$$

$$\dot{V}_3^{(8)} = \frac{1}{\dot{Y}_{33}} \cdot \left[\left(\frac{\dot{S}_3^{(8)}}{\dot{V}_3^{(7)}} \right)^* - \dot{Y}_{31} \cdot \dot{V}_1^{(8)} - \dot{Y}_{32} \cdot \dot{V}_2^{(8)} \right]$$

$$\dot{V}_3^{(8)} = \frac{1}{4,5454\angle -90} \cdot \left[\left(\frac{-0,24 + j0,0557}{0,95\angle -9,6169} \right)^* - 0 \cdot (1\angle 0) - (4,5454\angle 90) \cdot (0,9386\angle -6,3748) \right]$$

$$\dot{V}_3^{(8)} = 0,9500\angle -9,7675$$

Por lo tanto:

$$\dot{V}_3^{(8)} = 0.95\angle -9,7675 \text{ (p.u)}$$

$$\dot{V}_2^{(8)} = 0,9386\angle - 6,3748 \text{ (p.u)}$$

$$\dot{V}_3^{(8)} = 0,95\angle - 9,7675 \text{ (p.u)}$$

Para K = 8, nos queda:

$$\dot{V}_p^{(k+1)} = \frac{1}{\dot{Y}_{pp}} \cdot \left[\left(\frac{\dot{S}_p}{\dot{V}_p^{(k)}} \right)^* - \sum_{q=1}^{p-1} \dot{Y}_{pq} \cdot \dot{V}_q^{(k+1)} - \sum_{q=p+1}^n \dot{Y}_{pq} \cdot \dot{V}_q^{(k)} \right]$$

$$\dot{V}_2^{(9)} = \frac{1}{\dot{Y}_{22}} \cdot \left[\left(\frac{\dot{S}_2}{\dot{V}_2^{(8)}} \right)^* - \sum_{q=1}^1 \dot{Y}_{2q} \cdot \dot{V}_q^{(9)} - \sum_{q=3}^3 \dot{Y}_{2q} \cdot \dot{V}_q^{(8)} \right]$$

$$\dot{V}_2^{(9)} = \frac{1}{\dot{Y}_{22}} \cdot \left[\left(\frac{\dot{S}_2}{\dot{V}_2^{(8)}} \right)^* - \dot{Y}_{21} \cdot \dot{V}_1^{(9)} - \dot{Y}_{23} \cdot \dot{V}_3^{(8)} \right]$$

$$\dot{V}_2^{(9)} = \frac{1}{7,1109\angle - 80,1873} \cdot \left[\left(\frac{-0,09 - j0,0435}{(0,9386\angle - 6,3748)} \right)^* - (2,7435\angle 116,2136) \cdot (1\angle 0) - (4,5454\angle 90) \cdot (0,95\angle - 9,7675) \right]$$

$$\dot{V}_2^{(9)} = 0,9382\angle - 6,4689 \text{ (p.u)}$$

$$Q_p^{(k+1)} = -Im \left[\left(\dot{V}_p^{(k)} \right)^* \cdot \left(\sum_{q=1}^{p-1} \dot{Y}_{pq} \cdot \dot{V}_q^{(k+1)} + \sum_{q=p}^n \dot{Y}_{pq} \cdot \dot{V}_q^{(k)} \right) \right]$$

$$Q_3^{(9)} = -Im \left[\left(\dot{V}_3^{(8)} \right)^* \cdot \left(\sum_{q=1}^2 \dot{Y}_{3q} \cdot \dot{V}_q^{(9)} + \sum_{q=3}^3 \dot{Y}_{3q} \cdot \dot{V}_q^{(8)} \right) \right]$$

$$Q_3^{(9)} = -Im \left[\left(\dot{V}_3^{(8)} \right)^* \cdot \left(\dot{Y}_{31} \cdot \dot{V}_1^{(9)} + \dot{Y}_{32} \cdot \dot{V}_2^{(9)} + \dot{Y}_{33} \cdot \dot{V}_3^{(8)} \right) \right]$$

$$Q_3^{(9)} = -Im[(0,95\angle - 9,7675)^* \cdot (0 \cdot (1\angle 0) + (4,5454\angle 90^\circ) \cdot (0,9382\angle - 6,4689) + (4,5454\angle - 90) \cdot (0,95\angle - 9,7675))]$$

$$Q_3^{(9)} = 0,0577 \text{ (p.u)}$$

$$S_3^{(k+1)} = -0,24 + jQ_3^{(k+1)}$$

$$Q_{BC}^{(k+1)} = Q_3^{(k+1)} + 0,18 \text{ (p.u)}$$

$$Q_{BC}^{(9)} = Q_3^{(9)} + 0,18 \text{ (p.u)} = 0,2377 \text{ (p.u)}$$

$$S_3^{(9)} = -0,24 + jQ_3^{(9)} = -0,24 + j0,0577 \text{ (p.u)} = 0,2468\angle 166,4816 \text{ (p.u)}$$

$$\dot{V}_p^{(k+1)} = \frac{1}{\dot{Y}_{pp}} \cdot \left[\left(\frac{\dot{S}_p^{(k+1)}}{\dot{V}_p^{(k)}} \right)^* - \sum_{q=1}^{p-1} \dot{Y}_{pq} \cdot \dot{V}_q^{(k+1)} - \sum_{q=p+1}^n \dot{Y}_{pq} \cdot \dot{V}_q^{(k)} \right]$$

$$\dot{V}_3^{(9)} = \frac{1}{\dot{Y}_{33}} \cdot \left[\left(\frac{\dot{S}_3^{(9)}}{\dot{V}_3^{(8)}} \right)^* - \sum_{q=1}^2 \dot{Y}_{3q} \cdot \dot{V}_q^{(9)} - \sum_{q=4}^3 \dot{Y}_{3q} \cdot \dot{V}_q^{(8)} \right]$$

$$\dot{V}_3^{(9)} = \frac{1}{\dot{Y}_{33}} \cdot \left[\left(\frac{\dot{S}_3^{(9)}}{\dot{V}_3^{(8)}} \right)^* - \dot{Y}_{31} \cdot \dot{V}_1^{(9)} - \dot{Y}_{32} \cdot \dot{V}_2^{(9)} \right]$$

$$\dot{V}_3^{(9)} = \frac{1}{4,5454\angle -90} \cdot \left[\left(\frac{-0,24 + j0,0577}{0,95\angle -9,7675} \right)^* - 0 \cdot (1\angle 0) - (4,5454\angle 90) \cdot (0,9382\angle -6,4689) \right]$$

$$\dot{V}_3^{(9)} = 0,9500\angle -9,8638$$

Por lo tanto:

$$\dot{V}_3^{(9)} = 0.95\angle -9,8638 \text{ (p.u)}$$

$$\dot{V}_2^{(9)} = 0,9382\angle - 6,4689 \text{ (p.u)}$$

$$\dot{V}_3^{(9)} = 0,95\angle - 9,8638 \text{ (p.u)}$$

Para K = 9, nos queda:

$$\dot{V}_p^{(k+1)} = \frac{1}{\dot{Y}_{pp}} \cdot \left[\left(\frac{\dot{S}_p}{\dot{V}_p^{(k)}} \right)^* - \sum_{q=1}^{p-1} \dot{Y}_{pq} \cdot \dot{V}_q^{(k+1)} - \sum_{q=p+1}^n \dot{Y}_{pq} \cdot \dot{V}_q^{(k)} \right]$$

$$\dot{V}_2^{(10)} = \frac{1}{\dot{Y}_{22}} \cdot \left[\left(\frac{\dot{S}_2}{\dot{V}_2^{(9)}} \right)^* - \sum_{q=1}^1 \dot{Y}_{2q} \cdot \dot{V}_q^{(10)} - \sum_{q=3}^3 \dot{Y}_{2q} \cdot \dot{V}_q^{(9)} \right]$$

$$\dot{V}_2^{(10)} = \frac{1}{\dot{Y}_{22}} \cdot \left[\left(\frac{\dot{S}_2}{\dot{V}_2^{(9)}} \right)^* - \dot{Y}_{21} \cdot \dot{V}_1^{(10)} - \dot{Y}_{23} \cdot \dot{V}_3^{(9)} \right]$$

$$\dot{V}_2^{(10)} = \frac{1}{7,1109\angle - 80,1873} \cdot \left[\left(\frac{-0,09 - j0,0435}{(0,9382\angle - 6,4689)} \right)^* - (2,7435\angle 116,2136) \cdot (1\angle 0) - (4,5454\angle 90) \cdot (0,95\angle - 9,8638) \right]$$

$$\dot{V}_2^{(10)} = 0,9380\angle - 6,5290 \text{ (p.u)}$$

$$Q_p^{(k+1)} = -Im \left[\left(\dot{V}_p^{(k)} \right)^* \cdot \left(\sum_{q=1}^{p-1} \dot{Y}_{pq} \cdot \dot{V}_q^{(k+1)} + \sum_{q=p}^n \dot{Y}_{pq} \cdot \dot{V}_q^{(k)} \right) \right]$$

$$Q_3^{(10)} = -Im \left[\left(\dot{V}_3^{(9)} \right)^* \cdot \left(\sum_{q=1}^2 \dot{Y}_{3q} \cdot \dot{V}_q^{(10)} + \sum_{q=3}^3 \dot{Y}_{3q} \cdot \dot{V}_q^{(9)} \right) \right]$$

$$Q_3^{(10)} = -Im \left[\left(\dot{V}_3^{(9)} \right)^* \cdot \left(\dot{Y}_{31} \cdot \dot{V}_1^{(10)} + \dot{Y}_{32} \cdot \dot{V}_2^{(10)} + \dot{Y}_{33} \cdot \dot{V}_3^{(9)} \right) \right]$$

$$Q_3^{(10)} = -Im[(0,95\angle - 9,8638)^* \cdot (0 \cdot (1\angle 0) + (4,5454\angle 90^\circ) \cdot (0,9380\angle - 6,5290) + (4,5454\angle - 90) \cdot (0,95\angle - 9,8638))]$$

$$Q_3^{(10)} = 0,0587 \text{ (p.u)}$$

$$S_3^{(k+1)} = -0,24 + jQ_3^{(k+1)}$$

$$Q_{BC}^{(k+1)} = Q_3^{(k+1)} + 0,18 \text{ (p.u)}$$

$$Q_{BC}^{(10)} = Q_3^{(10)} + 0,18 \text{ (p.u)} = 0,2387 \text{ (p.u)}$$

$$S_3^{(10)} = -0,24 + jQ_3^{(10)} = -0,24 + j0,0587 \text{ (p.u)} = 0,2470\angle 166,2562 \text{ (p.u)}$$

$$\dot{V}_p^{(k+1)} = \frac{1}{\dot{Y}_{pp}} \cdot \left[\left(\frac{\dot{S}_p^{(k+1)}}{\dot{V}_p^{(k)}} \right)^* - \sum_{q=1}^{p-1} \dot{Y}_{pq} \cdot \dot{V}_q^{(k+1)} - \sum_{q=p+1}^n \dot{Y}_{pq} \cdot \dot{V}_q^{(k)} \right]$$

$$\dot{V}_3^{(10)} = \frac{1}{\dot{Y}_{33}} \cdot \left[\left(\frac{\dot{S}_3^{(10)}}{\dot{V}_3^{(9)}} \right)^* - \sum_{q=1}^2 \dot{Y}_{3q} \cdot \dot{V}_q^{(10)} - \sum_{q=4}^3 \dot{Y}_{3q} \cdot \dot{V}_q^{(9)} \right]$$

$$\dot{V}_3^{(10)} = \frac{1}{\dot{Y}_{33}} \cdot \left[\left(\frac{\dot{S}_3^{(10)}}{\dot{V}_3^{(9)}} \right)^* - \dot{Y}_{31} \cdot \dot{V}_1^{(10)} - \dot{Y}_{32} \cdot \dot{V}_2^{(10)} \right]$$

$$\dot{V}_3^{(10)} = \frac{1}{4,5454\angle -90} \cdot \left[\left(\frac{-0,24 + j0,0587}{0,95\angle -9,8638} \right)^* - 0 \cdot (1\angle 0) - (4,5454\angle 90) \cdot (0,9380\angle -6,5290) \right]$$

$$\dot{V}_3^{(10)} = 0,9500\angle -9,9251$$

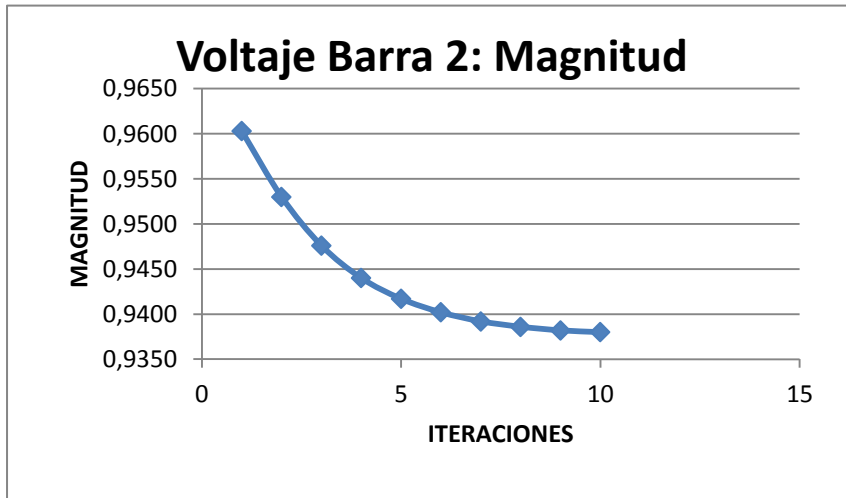
Por lo tanto:

$$\dot{V}_3^{(10)} = 0.95\angle -9,9251 \text{ (p.u)}$$

2. Graficar:

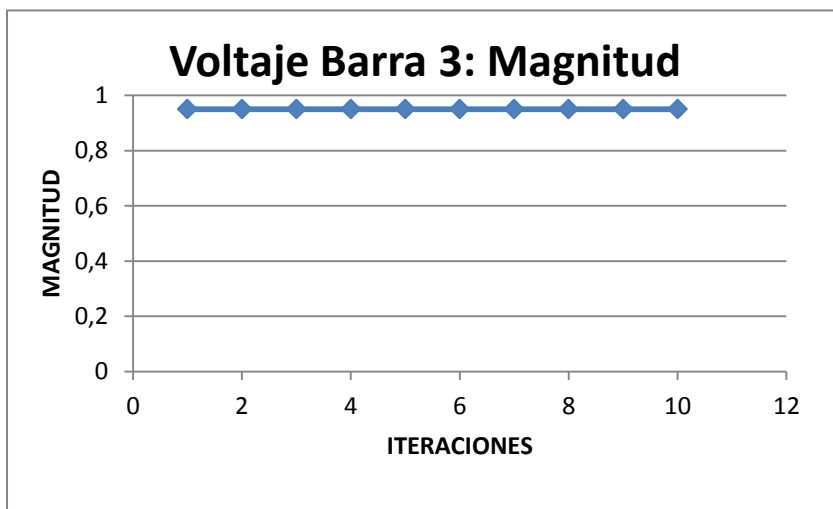
- La magnitud del voltaje en la Barra 2
- La magnitud del voltaje en la Barra 3
- El ángulo del voltaje en la Barra 2
- El ángulo del voltaje en la Barra 3
- La potencia reactiva Q_3
- La potencia reactiva Q_{BC}

1. Magnitud del voltaje en la Barra 2 (p.u.)



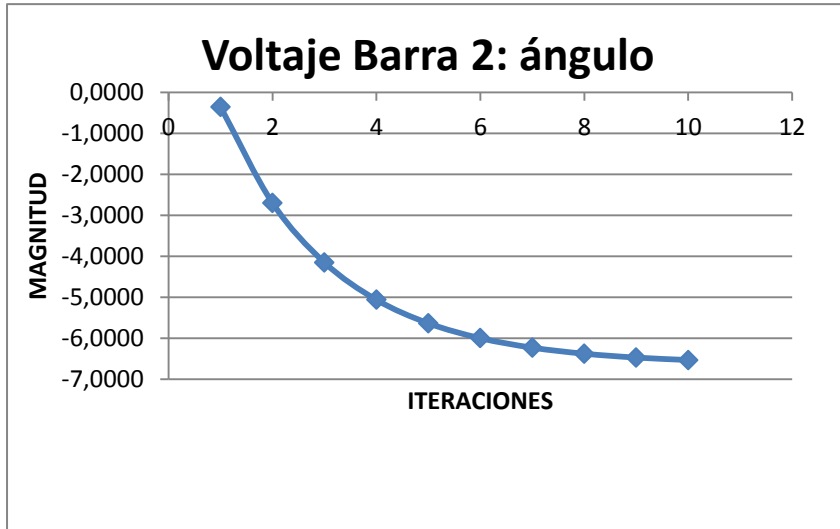
Iteración	Voltaje Barra 2: Magnitud
1	0,9603
2	0,9530
3	0,9476
4	0,9440
5	0,9417
6	0,9402
7	0,9392
8	0,9386
9	0,9382
10	0,9380

2. Magnitud del voltaje en la Barra 3 (p.u.)



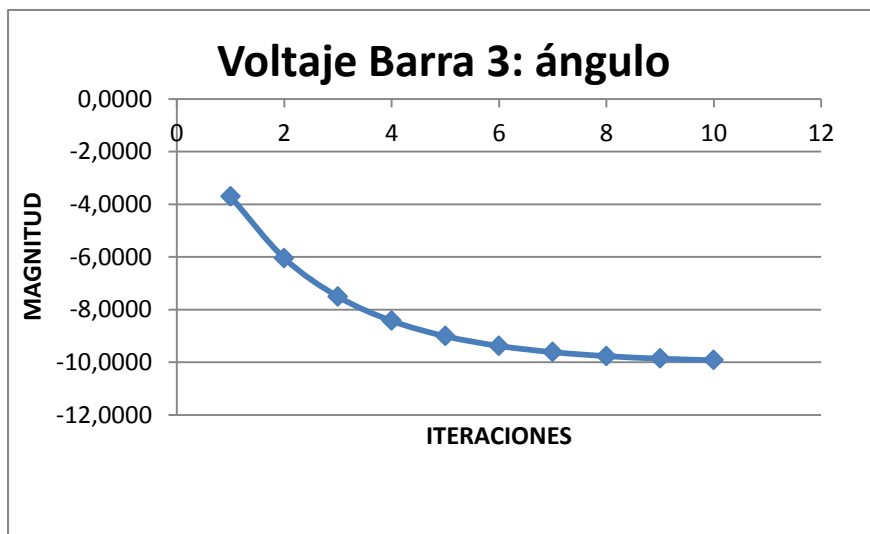
Iteración	Voltaje Barra 3: Magnitud
1	0,95
2	0,95
3	0,95
4	0,95
5	0,95
6	0,95
7	0,95
8	0,95
9	0,95
10	0,95

3. Ángulo del voltaje en la Barra 2 (p.u.)



Iteración	Voltaje Barra 2: ángulo
1	-0,3571
2	-2,6995
3	-4,1509
4	-5,0596
5	-5,6329
6	-5,9963
7	-6,2274
8	-6,3748
9	-6,4689
10	-6,5290

4. Ángulo del voltaje en la Barra 3 (p.u.)



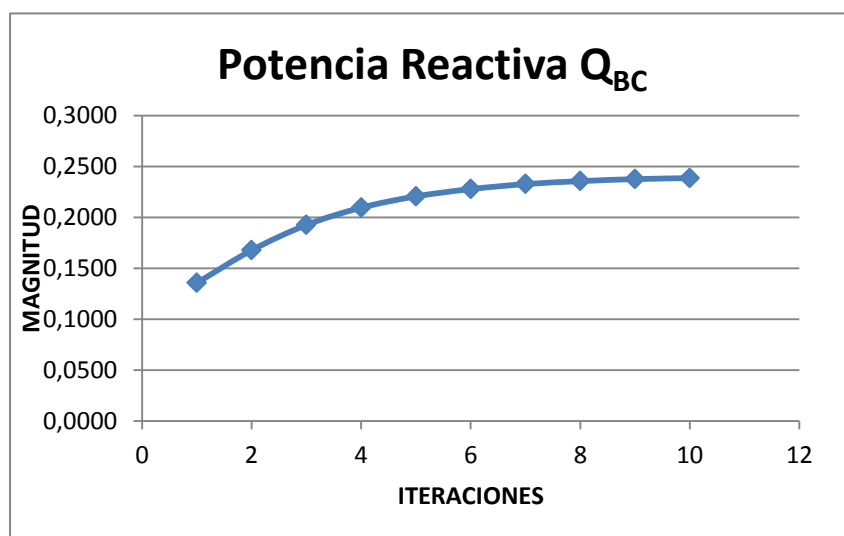
Iteración	Voltaje Barra 3: ángulo
1	-3,7079
2	-6,0471
3	-7,5078
4	-8,4278
5	-9,0105
6	-9,3808
7	-9,6169
8	-9,7675
9	-9,8638
10	-9,9251

5. Potencia reactiva Q_3 (p.u.)



Iteración	Potencia Reactiva Q_3
1	-0,0444
2	-0,0123
3	0,0126
4	0,0296
5	0,0407
6	0,0479
7	0,0528
8	0,0557
9	0,0577
10	0,0587

6. La potencia reactiva Q_{BC} (p.u.)



Iteración	Potencia Reactiva Q_{BC}
1	0,1356
2	0,1677
3	0,1926
4	0,2096
5	0,2207
6	0,2279
7	0,2328
8	0,2357
9	0,2377
10	0,2387